

A Charge Isolated Conductor

“An excess charge on an isolated conductor is located entirely on the outer sphere of the conductor.”

The electric intensity inside the conductor must be zero. Suppose a hollow conducting sphere of radius r . We place a Gaussian surface inside hollow charged sphere.

Applying Gauss law,

$$\Phi_E = \frac{q}{\epsilon_0}$$

We know $q = 0$ inside Gaussian surface.

$$\Phi_E = \frac{0}{\epsilon_0}$$

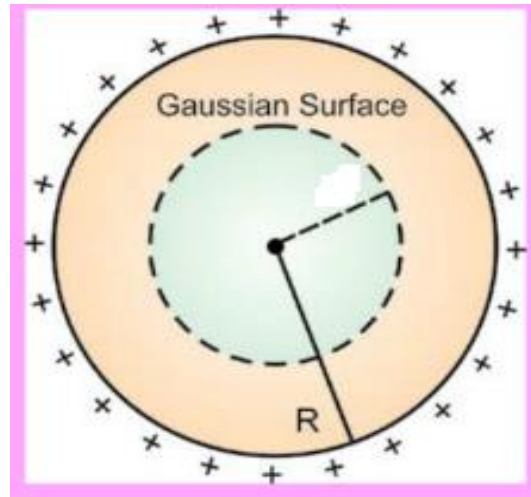
$$\text{Also } \Phi_E = \vec{E} \cdot \vec{A}$$

$$\vec{E} \cdot \vec{A} = 0$$

$$\vec{A} \neq 0, \vec{E} = 0$$

Result:

Thus any apparatus placed within a charge isolated conductor is “shielded” from electric field.



A Spherically Symmetric Charge Distribution

The external electric field near the surface of charged conductor is perpendicular to the surface and has a magnitude that depends on the surface charge density σ

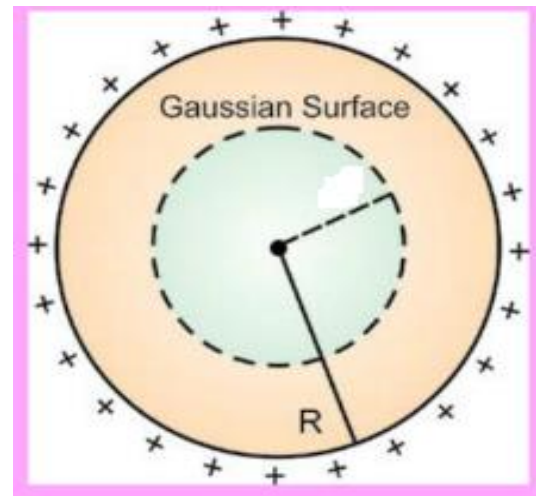
$$E = \frac{\sigma}{\epsilon_0}$$

Within the conductor $E = 0$

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Applying Gauss law,



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$$\text{Also } \Phi_E = \vec{E} \cdot \vec{A}$$

$$\vec{E} \cdot \vec{A} = 0$$

$$\vec{A} \neq 0, \vec{E} = 0$$

Thus any apparatus placed within a charge isolated conductor is “shielded” from electric field.

Suppose a spherical Gaussian surface outside the hollow conducting sphere. There is uniform surface charge density σ

$$\sigma = \frac{q}{A} \Rightarrow q = \sigma A$$

Applying Gauss law to find out electric intensity outside a spherically symmetric charge distribution.

$$\Phi_E = \frac{q}{\epsilon_0} = \frac{\sigma A}{\epsilon_0}$$

Also we have

$$\Phi_E = \vec{E} \cdot \vec{A}$$

$$\text{Then } \vec{E} \cdot \vec{A} = \frac{\sigma A}{\epsilon_0}$$

$$E = \frac{\sigma}{\epsilon_0}$$

Result:

The external electric field near the surface of charged conductor is perpendicular to the surface and has a magnitude that depends on the surface charge density σ

$$E = \frac{\sigma}{\epsilon_0}$$

Within the conductor $E = 0$.

